

Pre-Calculus
Unit 1 Functions Guiding Questions

Name _____
 Hour _____

- Equations such as $A = 40x - x^2$ and $h = 300 - 16t^2$ define quadratic functions. The word function means that assigning a value to one of the variables (x or t) determines a unique value for the other (A or h). It is customary to say that "A is a function of x ." In this example, however, it would be incorrect to say that " x is a function of A ." Explain.
- A hose used by the fire department shoots water out in a parabolic arc. Let x be the horizontal distance from the hose's nozzle, and y be the corresponding height of the stream of water, both in feet. The quadratic function is $y = -0.016x^2 + 0.5x + 4.5$.
 - What is the significance of the 4.5 that appears in the equation?
 - Find the stream's greatest height.
 - What is the horizontal distance from the nozzle to where the stream hits the ground?
 - Will the stream go over a 6-foot high fence that is located 28 feet from the nozzle?
 - Sketch a graph of the function.
- Sketch the graphs of $f(x) = (x - 4)^2$ and $g(x) = (4 - x)^2$. What do you notice about the graphs? Explain why this is true.
- The three functions $y = 2(x - 4) - 1$, $y = 2|x - 4| - 1$ and $y = 2(x - 4)^2 - 1$ look somewhat similar. Predict what the graph of each will look like, and then sketch them by hand by plotting a few key points. In each case, think about how the form of the equation can help provide information.
- Determine the domain and range of $f(x) = \frac{x^2 - 1}{x + 1}$.
- Determine the domain and range of $y = -2\sqrt{2x - 3} + 2$.
- The IRS Tax Formula for married couples in the year 2013 is given by the linear-piecewise function below:

$$T(x) = \begin{cases} 0.1x & \text{for } 0 \leq x \leq 17850 \\ 1785 + 0.15(x - 17850) & \text{for } 17850 < x \leq 72500 \\ 9982.5 + 0.25(x - 72500) & \text{for } 72500 < x \leq 146400 \\ 28457.5 + 0.28(x - 146400) & \text{for } 146400 < x \leq 223050 \\ 49919.5 + 0.33(x - 223050) & \text{for } 223050 < x \leq 398350 \\ 107768.5 + 0.35(x - 398350) & \text{for } 398350 < x \leq 450000 \\ 125846 + 0.396(x - 450000) & \text{for } 450000 < x \end{cases}$$

- What does x represent?
 - What does $T(x)$ represent?
 - Determine the tax owed for a married couple whose income is \$76,423 annually.
 - Is this function continuous on the domain?
- Given the graph of the function $f(x)$. Sketch the inverse of the graph.
 - Find a function f for which $f(x+3)$ is not equivalent to $f(x) + f(3)$.
 - Find a function f for which $f(x+3)$ is equivalent to $f(x) + f(3)$.
 - What is the result of graphing the equation $(x - h)^2 + (y - k)^2 = r^2$? Where h , k and r are integers.
 - Write an equation that describes all the points on the circle whose center is at the origin and whose radius is (a) 13; (b) 6 and (c) r
 - Graph the circle whose equation is $x^2 + y^2 = 64$. What is its radius? What do the equations $x^2 + y^2 = 1$, $x^2 + y^2 = 40$ and $x^2 + y^2 = k$ all have in common? How do they differ?

